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Magnetic field-induced ferroelectricity in  $S = 1/2$  kagome staircase compound  $\text{PbCu}_3\text{TeO}_7$ Kyongjun Yoo<sup>1</sup>, B. Koteswararao<sup>1,2</sup>, Jeonghun Kang<sup>1</sup>, Aga Shahee<sup>1</sup>, Woohyun Nam<sup>1</sup>, Fedor F. Balakirev<sup>3</sup>, Vivien S. Zapf<sup>3</sup>, Neil Harrison<sup>3</sup>, Alexander Guda<sup>4</sup>, Nikita Ter-Oganessian<sup>5</sup> and Kee Hoon Kim<sup>1</sup>

$\text{Ni}_3\text{V}_2\text{O}_8$  is an archetypical multiferroic material with a kagome staircase structure of  $S = 1$  ( $\text{Ni}^{2+}$ ) spins whose complex interplay between spin ordering and ferroelectricity has been studied for more than a decade. Here, we report a new kagome staircase compound  $\text{PbCu}_3\text{TeO}_7$  with  $\text{Cu}^{2+}$  ( $S = 1/2$ ) spins that exhibits two Néel temperatures at  $T_{\text{N}1} = 36$  K and  $T_{\text{N}2} = 24$  K, and a magnetic field ( $H$ )-induced electric polarization ( $P$ ) below  $T_{\text{N}2}$ . Pyroelectric and magnetoelectric current measurements in magnetic fields up to 60 T reveal that for  $H \parallel c$  of  $\sim 8.3$  T, a spin-flop transition induces a transverse  $P \parallel a$  with a magnitude of  $15 \mu\text{C}/\text{m}^2$  below  $T_{\text{N}2}$ . Furthermore, for a parallel configuration with  $P \parallel H \parallel a$ , two spin-flop transitions occur, the first at  $\sim 16$  T with  $P \parallel a$  of  $14 \mu\text{C}/\text{m}^2$ , and the second at  $\sim 38$  T, where  $P$  disappears. Monte Carlo simulations based on 12 major exchange interactions uncover that a sinusoidal amplitude modulation of the spins occurs along the  $b$ -axis below  $T_{\text{N}1}$  and an incommensurate, proper screw-type spin order occurs in the  $ac$ -plane below  $T_{\text{N}2}$ . The simulation results show that  $P \parallel a$  under  $H \parallel c$  stems from a spin-flop transition facilitating an  $ab$ -plane-type spiral order, while the two successive spin-flop transitions for  $H \parallel a$  result in spiral spin orders in the  $ab$ - and  $bc$ -planes. Based on the experimental and theoretical results, we establish field-induced magnetic and electric phase diagrams for the two  $H$  directions, demonstrating that the distorted kagome staircase structure with competing intra–interlayer interactions and lifted frustration creates a plethora of different noncollinear spin textures of  $S = 1/2$  spins that in turn induce electric polarization.

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## INTRODUCTION

Research activities on multiferroics and magnetoelectric (ME) materials have resumed since early 2000s because of the fundamental interests in the physics of strong coupling between spin and lattice degrees of freedom as well as the application potential for numerous low-power electronic devices.<sup>1–5</sup> In particular, magnetic ferroelectrics, in which ferroelectric polarization ( $P$ ) is induced by spin order, have drawn lots of attention due to the intriguing complexity of the spin textures and magnetoelectric coupling mechanisms, as well as the ability to control 100% of the electric polarization with magnetic ordering. In magnetic ferroelectrics, one route to creating ferroelectricity is via competing magnetic interactions that induce complex nontrivial spin orders. These complex spin orders in turn break spatial inversion symmetry of the combined spin-lattice system and thus induce  $P$ .<sup>4,5</sup> For example, ferroelectricity observed in quasi-one-dimensional spin chain compounds  $\text{MnWO}_4$ ,<sup>6</sup>  $\text{Ca}_3\text{Co}_{1.04}\text{Mn}_{0.96}\text{O}_6$ ,<sup>7</sup> and  $\text{Lu}_2\text{CoMnO}_6$ <sup>8</sup> can be explained by such complex spin orders induced by the competing nearest and next-nearest neighbor exchange interactions.

Another effective way to realize complex spin orders is to make use of “lifted frustration”. In geometrically frustrated lattice such as triangular, kagome, or spinel structures, the frustration is so complete that no single ordered ground state can occur in theory,

giving rise to classical or quantum-spin liquids. However, in real systems, the perfect spin frustration is often lifted by symmetry-reducing lattice distortions that eventually lead to spontaneous spin ordering at finite temperatures. These lattice distortions can directly cause ferroelectricity, or the resulting spin orderings are also sufficiently complex as to induce electric polarization, as occurs, e.g., in  $\text{Ni}_3\text{V}_2\text{O}_8$ ,<sup>9–14</sup>  $\text{CuFeO}_2$ ,<sup>15,16</sup>  $\text{CoCr}_2\text{O}_4$ ,<sup>17</sup> and  $\text{AgCrO}_2$ .<sup>18</sup>

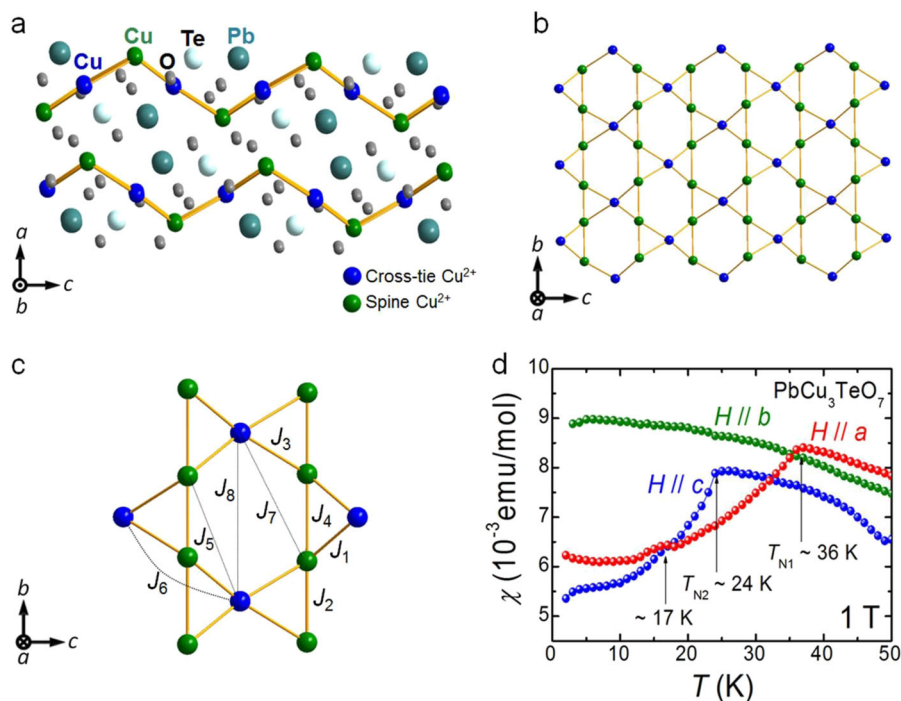
Among geometrically frustrated lattices,<sup>6–8</sup> the kagome structure has received particular attention since it is a prime candidate for creating quantum-spin-liquid states.<sup>19</sup> Numerous studies<sup>20,21</sup> have mainly focused on the quest for a possible quantum-spin-liquid ground state in the ideal kagome lattices, whereas multiferroic properties have not been extensively studied.  $\text{Ni}_3\text{V}_2\text{O}_8$ , however, is a rare example of exhibiting multiferroic behavior in a distorted kagome structure. Here,  $\text{Ni}^{2+}$  ( $S = 1$ ) spins organize into a buckled form of the kagome structure, called as the kagome staircase structure. Extensive studies on  $\text{Ni}_3\text{V}_2\text{O}_8$  have now made significant progresses in understanding its intriguing ME coupling and complex phase diagram.<sup>9–14</sup> Upon being cooled,  $\text{Ni}_3\text{V}_2\text{O}_8$  exhibits four magnetic phases below 9.3 K; high- and low-temperature incommensurate (HTI and LTI) and two commensurate ones. Among those, ferroelectricity has been found only in the LTI phase, in which neutron scattering studies<sup>9,12</sup> have revealed stabilization of a spin cycloid structure in the  $ab$ -plane. Therefore, the origin of spontaneous  $P$  is now understood as

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**Fig. 1** Crystal structure and magnetic susceptibility of  $\text{PbCu}_3\text{TeO}_7$  single crystals. Crystal structures viewed along **a** the b-axis with all atoms and along **b** the a-direction showing the staircase kagome structure with spine Cu ions (green) and cross-tie Cu ions (blue). **c** Possible intralayer exchange interactions denoted from  $J_1$  to  $J_8$  in the order of the distance. **d** Temperature-dependent magnetic susceptibility data along each field direction

coming from the so-called inverse Dzyaloshinskii–Moriya (IDM) mechanism.<sup>22–24</sup>

In terms of multiferroics/ME properties, the  $S=1/2$  system containing  $\text{Cu}^{2+}$  ions has drawn continual interest because strong quantum fluctuation effects expected from the smallest possible spin value may show up in the magnetic and multiferroic properties.<sup>25,26</sup> Moreover, some of the  $\text{Cu}^{2+}$ -containing compounds have high spin ordering temperatures because of their strong superexchange interaction arising from Cu–O–Cu bonding.<sup>27,28</sup> A number of multiferroic/ME compounds with  $S=1/2$  chains were indeed found;  $\text{LiCu}_2\text{O}_2$ ,<sup>25</sup>  $\text{SrCuTe}_2\text{O}_6$ ,<sup>26</sup>  $\text{CuO}$ ,<sup>27</sup>  $\text{CuBr}_2$ ,<sup>28</sup>  $\text{LiCuVO}_4$ ,<sup>29</sup>  $\text{CuCrO}_4$ ,<sup>30</sup>  $\text{CuCl}_2$ ,<sup>31</sup>  $\text{PbCuSO}_4(\text{OH})_2$ ,<sup>32</sup>  $\text{Cu}_3\text{Mo}_2\text{O}_9$ ,<sup>33</sup>  $\alpha\text{-Cu}_2\text{V}_2\text{O}_7$ ,<sup>34</sup>  $\text{Cu}_3\text{Nb}_2\text{O}_8$ ,<sup>35</sup>  $\text{Cu}_3\text{Bi}(\text{SeO}_3)_2\text{O}_2\text{Cl}$ ,<sup>36</sup> and  $\text{KCu}_3\text{As}_2\text{O}_7(\text{OD})_3$ .<sup>37,38</sup> Most of these compounds listed in refs. 25–38 share a common feature of  $\text{CuO}_2$  ribbons with edge-sharing  $\text{CuO}_4$  square planes. Therefore, the nearest-neighbor spin interaction through the Cu–O–Cu path can compete with the next-nearest neighbor interaction through the Cu–O–O–Cu path, resulting in a cycloidal spin order. Spontaneous  $P$  can then be induced by the IDM mechanism.<sup>22–24</sup> Moreover, recently known multiferroic compound  $\text{KCu}_3\text{As}_2\text{O}_7(\text{OD})_3$  has a monoclinically distorted kagome structure, which allows long-range spin order with a cycloidal configuration.<sup>37,38</sup> However, to our knowledge, no ME or multiferroic behaviors have been found to date in the staircase kagome spin structure with  $S=1/2$   $\text{Cu}^{2+}$  ions, which could open a new route to find exotic magnetic and multiferroic phenomena due to its unique opportunity of having quantum fluctuation, geometric spin frustration, and competing nearest- and next-nearest spin interaction all in one spin network.

We have recently found that  $\text{Cu}^{2+}$  ( $S=1/2$ ) ions in one of emergent copper tellurium oxides  $\text{PbCu}_3\text{TeO}_7$ ,<sup>39–41</sup> form the kagome staircase structure. The previous studies of magnetization,<sup>39</sup> heat capacity,<sup>39</sup> and nuclear magnetic resonance (NMR) studies<sup>40</sup> have shown that  $\text{PbCu}_3\text{TeO}_7$  has two antiferromagnetic (AFM) transitions at  $T_{N1}=36$  K and  $T_{N2}=24$  K and a small change in the magnetic susceptibility at  $T_{N3}=17$  K. The Curie–Weiss

temperature  $\theta_{\text{CW}}=-150$  K obtained from the magnetic susceptibility indicated the presence of moderate spin frustration. In addition, strong interlayer interactions through the Cu–O–Te–O–Cu path were evident in the NMR measurement.<sup>40</sup> This observation indicates that we should expect not only highly frustrated intralayer spin interactions, but also competing next-nearest exchange interaction via the strong interlayer coupling. Therefore,  $\text{PbCu}_3\text{TeO}_7$  is a good candidate material for exhibiting the noncollinear spin order and magnetism-induced ferroelectricity.

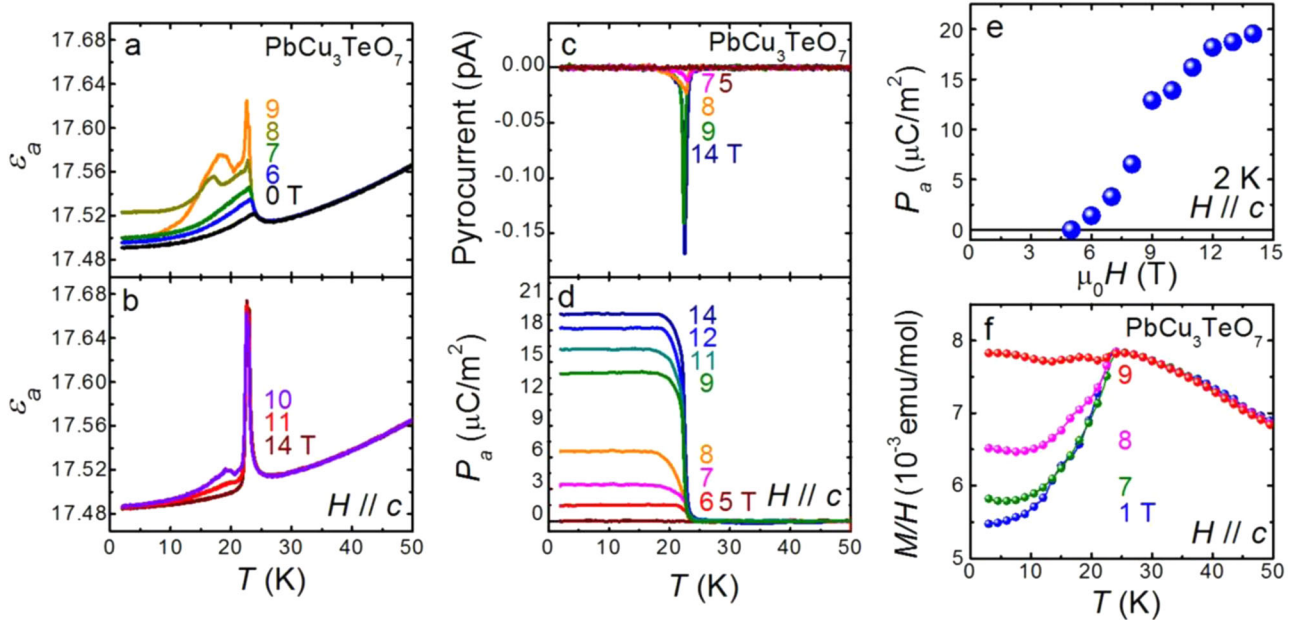
In this article, we report the observation of magnetic-field ( $H$ )-induced ferroelectricity in  $\text{PbCu}_3\text{TeO}_7$ . We find that below  $T_{N2}=24$  K,  $P_a$  is generated for transverse  $\mu_0 H_c > 8.3$  T and longitudinal  $16\text{ T} < \mu_0 H_a < 38\text{ T}$ , due to spin-flop (SF) transitions. We establish the phase diagram of  $\text{PbCu}_3\text{TeO}_7$  for each  $H$  direction based on the electric and magnetic properties. Based on the exchange interactions obtained by the first-principles calculation, Monte Carlo (MC) simulations were performed to reveal spin configurations in each phase. Our calculations suggest that the  $P_a$  generated by  $\mu_0 H_c > 8.3$  T and  $16\text{ T} < \mu_0 H_a < 38\text{ T}$  stems from a cycloid spin phase rotating in the  $ab$ -plane.

## RESULTS

$\text{PbCu}_3\text{TeO}_7$  crystallizes in an orthorhombic structure ( $Pnma$  space group), in which Cu atoms form the two-dimensional kagome structure in the  $bc$ -plane (Fig. 1a, b). The kagome planes are buckled in a zigzag form to constitute the staircase kagome structure. The buckled kagome planes are also stacked along the  $a$ -direction and separated by Pb and Te atoms with a small interlayer distance of  $\sim 4$  Å. The lattice parameters were obtained from the Rietveld refinement of powder XRD patterns;  $a=10.484$  Å,  $b=6.347$  Å, and  $c=8.807$  Å.<sup>39</sup> First-principles calculation based on the density functional theory (DFT) were performed to determine the values of the possible exchange interactions. Figure 1c summarizes the main intraplane exchange interactions labeled

**Table 1.** Exchange parameters of  $\text{PbCu}_3\text{TeO}_7$  determined by the DFT calculation.  $J_n$  ( $n = 1-8$ ) refer to the intralayer exchange constants that appear in Fig. 1c, while  $J_{in}$  ( $n = 1-4$ ) represent the interlayer ones

	$J_1$	$J_2$	$J_3$	$J_4$	$J_5$	$J_6$
Cu–Cu distance, Å	2.901	3.066	3.264	3.287	5.433	5.616
$J_i$ , meV	-1.6	0.45	2.9	1.7	1.1	0.72
	$J_7$	$J_8$	$J_{i1}$	$J_{i2}$	$J_{i3}$	$J_{i4}$
Cu–Cu distance, Å	6.353	6.696	5.918	6.117	6.278	6.279
$J_i$ , meV	2.77	1.3	2.5	0.2	0.05	-3.3


**Fig. 2** Temperature dependence of the electric and magnetic properties of  $\text{PbCu}_3\text{TeO}_7$  for  $H//c$ . **a, b** Dielectric constant  $\epsilon//a$ , **c** pyroelectric current, **d** electric polarization  $P//a$ , and **f** magnetization divided by  $H$  at selected  $H//c$ . **e** Electric polarization at various  $H//c$  estimated at 2 K

from  $J_1$  to  $J_8$  in the order of the distance between neighboring Cu pairs [Four additional interplane exchange interactions are not plotted here, but are summarized in Table 1].

Figure 1d plots the magnetic susceptibility  $\chi(T)$  data measured along each crystallographic direction.  $\chi$  exhibits significant anisotropy consistent with the previous report by Koteswararao et al.<sup>39</sup> For  $H//a$ , there is an abrupt decrease of  $\chi$  below  $T_{N1} \sim 36$  K, signaling an AFM ordering, termed AFM 1. For  $H//c$ ,  $\chi$  starts to decrease below  $T_{N2} \sim 24$  K and eventually becomes lower than the  $\chi$  value measured along the  $a$ -axis, implying stabilization of another AFM ordering, termed AFM 2. However, for  $H//b$ ,  $\chi$  remains high without showing any anomaly. All these observations indicate that the crystallographic  $b$ -direction is the spin-hard axis in the two AFM phases, while the  $a$ -direction is the spin-easy axis in the AFM 1 phase. Moreover, with the stabilization of the AFM 2 phase, the crystallographic  $c$ -direction also becomes the spin-easy axis. Besides, a small kink is observed at  $\sim 17$  K in the  $\chi$  curve along  $H//a$ . It is also seen that the  $\chi(T)$  curves along  $H//a$  and  $H//c$  cross each other at the anomaly at  $\sim 17$  K.

Figure 2a–d present the electrical properties, i.e., the dielectric constant ( $\epsilon_a$ ), pyrocurrent  $I_p$ , and the corresponding electric polarization ( $P_a$ ) curves. All are measured along the  $a$ -direction in the  $H//c$  configuration ( $H_c$ ). In the low-field region (Fig. 2a), the  $\epsilon_a$  curve exhibits a small kink in the vicinity of  $T_{N2} \sim 24$  K. With increasing  $\mu_0 H_c$ , the kink feature grows and develops into a sharp

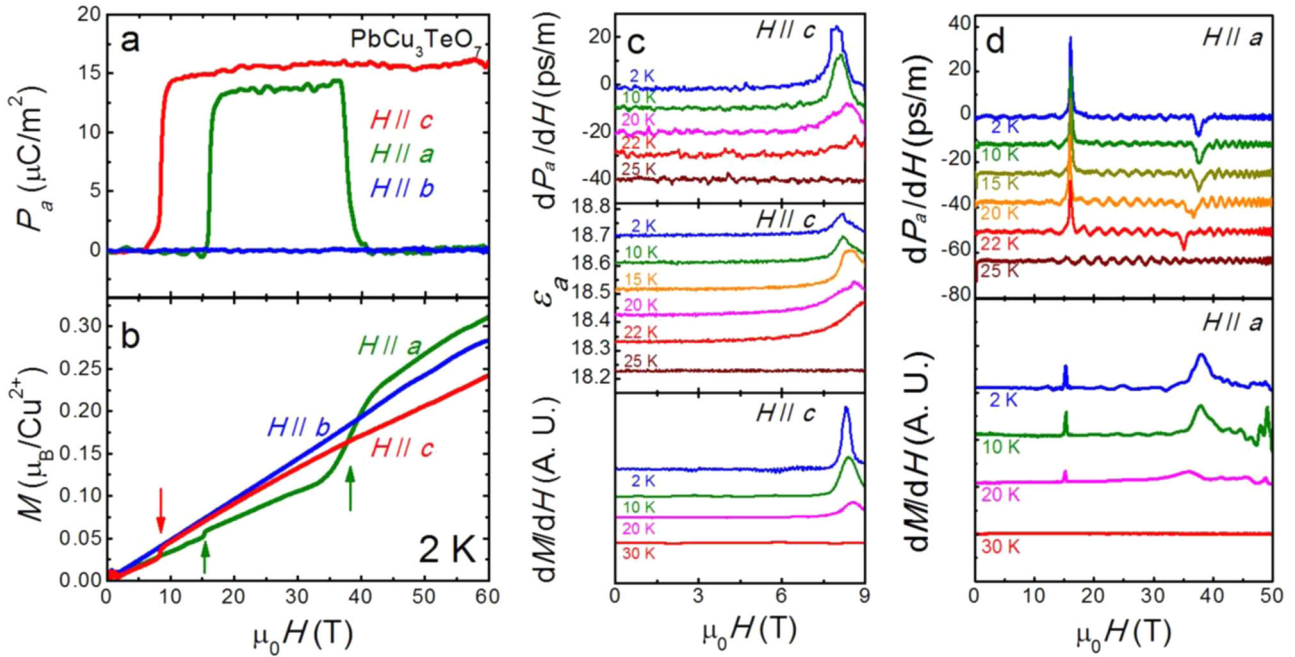
peak; the peak intensity starts to increase above 6 T, shows an abrupt jump at  $\mu_0 H_c = 9$  T, and becomes almost saturated for  $\mu_0 H_c \geq 10$  T (Fig. 2b). Finally, at the highest  $\mu_0 H_c = 14$  T,  $\epsilon_a$  exhibits the sharpest single peak. Consistent with this, we observe a dip feature in the  $I_p$  curves at  $\mu_0 H_c \geq \sim 6$  T (Fig. 2c). As the magnetic field increases beyond 8 T, the dip feature is progressively enhanced, exhibiting the most abrupt change between 8 and 9 T. Correspondingly, a finite  $P_a$  starts to appear at  $\mu_0 H_c \geq 6$  T and exhibits an abrupt increase between 8 and 9 T. The resultant  $P_a$  value at 2 K is summarized in Fig. 2e; it starts to appear at  $\mu_0 H_c \geq 6$  T, suddenly jumps between 8 and 9 T, and reaches the maximum value of  $19.5 \mu\text{C}/\text{m}^2$  at  $\mu_0 H_c = 14$  T. The temperature, where  $P_a$  starts to appear, almost coincides with  $T_{N2} = 24$  K, implying that the AFM 2 phase at  $\mu_0 H_c \geq 6$  T is also ferroelectric. The sign of  $I_p$  is

reversed after negative electric poling ( $-E_p$ ) (not shown here), supporting the existence of ferroelectricity at  $\mu_0 H_c \geq 6$  T. In addition, for magnetic fields up to 14 T, the dip feature in  $I_p$  was only observed in this particular electric and magnetic field configuration, i.e.,  $P//a$  and  $H//c$ .

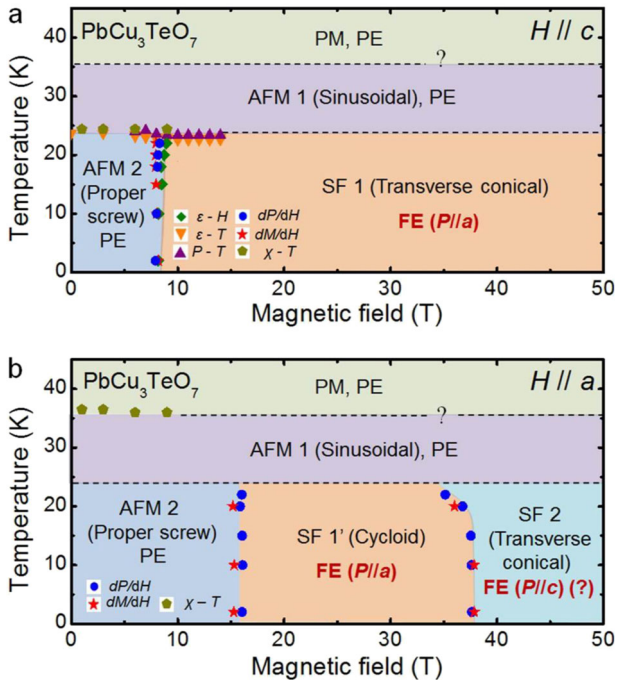
To further understand the spin configuration in the high-field region, the  $M/H$  curves are investigated along the  $c$ -axis in Fig. 2f at the bias fields  $\mu_0 H_c = 1, 7, 8,$  and  $9$  T. A sharp drop near  $T_{N2} \sim 24$  K in the  $M/H$  curve at  $\mu_0 H_c = 1$  T is consistent with the  $\chi(H//c)$  curve in Fig. 1d, pointing to the stabilization of the AFM 2 phase. When the bias field is increased, the  $M/H$  curves remain nearly unchanged up to 6 T, then increase conspicuously between  $\mu_0 H_c = 8$  and  $9$  T, and becomes almost temperature-independent at  $H_c = 9$  T. This could result from an SF transition in the vicinity of  $\mu_0 H_c = 8$  T. This observation is also consistent with the sharp increase of  $P_a$  between  $\mu_0 H_c = 8$  and  $9$  T. Such concomitant sharp increases of  $P_a$  and  $M/H$  values imply that the SF phase of AFM 2 is responsible for the induced  $P_a$  at  $\mu_0 H_c \geq 6$  T.

In order to check possible  $H$ -induced  $P_a$  changes in other crystallographic directions and also at higher fields, we used a pulsed magnetic field up to 60 T to investigate the  $H$ -dependent ME current, magnetization ( $M$ ), and  $\epsilon$  curves in various  $H$  directions. Figure 3a summarizes the  $P(H)$  curve at 2 K for every  $H$  direction as obtained from the integration of the ME current. For  $H//c$ ,  $P_a$  becomes finite at  $\sim 6$  T and abruptly increases up to  $\sim$





**Fig. 3** Magnetic-field dependence of the electric and magnetic properties of  $\text{PbCu}_3\text{TeO}_7$  single crystals. **a** Electric polarization ( $P_a$ ) and **b** magnetization  $M$  for each magnetic-field directions at 2 K. The arrows in the  $M$  curves indicate the potential SF transitions. ME coefficient ( $dP/dH$ ), dielectric constant ( $\epsilon//a$ ), and field derivative of magnetization ( $dM/dH$ ) at selected temperatures for **c**  $H//c$  and **d**  $H//a$ . For clarity, all the  $dP/dH$ ,  $\epsilon$ , and  $dM/dH$  curves above 2 K were shifted down by a vertical offset at each temperature



**Fig. 4** Temperature vs. magnetic-field phase diagram of  $\text{PbCu}_3\text{TeO}_7$  for **a**  $H//c$  and **b**  $H//a$ . The data points indicate the anomalies in the dielectric constant ( $\epsilon$ ), magnetization ( $M$ ), and electric polarization ( $P$ ). Below the PM (paramagnetic), PE (paraelectric) phase, there exist several ordered phases: AFM 1, AFM 2, SF 1, SF 1', SF 2, and FE (ferroelectric) phases

$15 \mu\text{C}/\text{m}^2$  at  $\sim 9$  T; this is consistent with the  $P_a$  data obtained from the DC magnetic fields from the  $I_p$  measurement up to 14 T in Fig. 2. In this pulsed magnetic field experiment, we have verified that  $P_a$  remains almost constant up to 60 T. Moreover, we found in the

$H//a$  ( $H_a$ ) measurement that  $P_a \sim 14 \mu\text{C}/\text{m}^2$  also develops at  $\mu_0 H_a \geq \sim 16$  T and decreases again from  $\mu_0 H_a = 36$  T to become zero at  $\mu_0 H_a = 41$  T. Finally, we found no  $P_a$  for  $H//b$ .

Figure 3b summarizes the corresponding magnetization  $M$  curve measured at 2 K obtained in pulsed magnetic fields up to 60 T.  $M$  increases linearly with  $H$  in the low-field region for each direction.  $M$  exhibits step-like increases at 8.3 T and 15.4 T for  $H//c$  and  $H//a$ , respectively. The linear extrapolations in both the  $M$  ( $H//c$ ) curve at  $\mu_0 H_c > 8.3$  T and the  $M$  ( $H//a$ ) curve at  $\mu_0 H_a > 15.4$  T result in a zero intercept at  $H = 0$ , implying that the spin ordering pattern realized at  $\mu_0 H_c > 8.3$  T and  $\mu_0 H_a > 15.4$  T in the high-field region is also AFM after the SF transition. In the configuration of  $H//a$ , an additional large step is observed at 38 T. The linearly extrapolated line along the  $M(H//a)$  curve at  $\mu_0 H_a > \sim 42$  T still passed the zero offset, implying that another type of SF transition occurs. In contrast, for  $H//b$ ,  $M$  increases linearly up to 60 T without any anomaly. Most importantly, in all the  $M$  vs.  $H$  curves presented in Fig. 3b, the fields where the SF transitions occur match those where the jumps in the  $P_a(H)$  curves are observed. This implies that the changes in the spin ordering pattern induced by the magnetic fields should be responsible for the  $P_a$  change. Furthermore, upon extrapolating the experimental magnetization data presented in Fig. 3b, we estimate the magnetic field for full saturation of magnetic moments to be  $\sim 120$ – $140$  T.

To determine the phase boundaries of the SF transitions as functions of the temperature and magnetic field, we investigated the field-derivative curves of  $P_a$  ( $dP_a/dH$ ) and  $M$  ( $dM/dH$ ), as summarized in Fig. 3c, d. For  $H//c$  (Fig. 3c), all the  $dP_a/dH$ ,  $dM/dH$ , and  $\epsilon_a$  curves exhibit a single sharp peak at the SF transition; their peak fields are consistent with each other and become almost temperature-independent. Moreover, the peaks are observed only below 24 K, proving that the SF transition occurs in the AFM 2 phase. The peak fields become higher at higher temperatures and eventually disappear at 24 K, which agrees with the temperature-dependent measurements shown in Fig. 2. The evolution of the peak fields can be clearly seen in Fig. 4a, in which the electric and magnetic phase diagram is presented for  $H_c$ .

However, for  $H//a$ , both  $dP_a/dH$  and  $dM/dH$  curves display either peak or dip at  $\mu_0 H_a = \sim 16$  T and  $\sim 38$  T, pointing to the two consecutive SF transitions. The peak position at  $\sim 16$  T in the  $dP_a/dH$  curve stays almost the same, while the second peak at  $\sim 38$  T shifts to lower fields upon warming up to 22 K. Furthermore, both peaks disappear above 24 K. The corresponding  $dM/dH$  curves exhibit a peak and a dip feature at almost same temperatures where the peaks in  $dP_a/dH$  are observed. The peak and dip feature also disappears above 24 K. This directly proves that these field-induced SF transitions occur only within the AFM 2 phase stabilized below 24 K. The evolution of the peak or dip locations in  $dM/dH$  is also summarized in the phase diagram of Fig. 4b.

Based on the data presented in Figs. 2 and 3, we plot the phase diagram of  $\text{PbCu}_3\text{TeO}_7$  for  $H//c$  and  $H//a$  in Fig. 4a, b, respectively. The peak positions in  $dP_a/dH$ ,  $dM/dH$ ,  $\epsilon_a(H)$ ,  $\epsilon_a(T)$ ,  $\chi(H)$ , and  $\chi(T)$  and the temperatures, at which  $P_a(T)$  starts to appear or disappear, are drawn. The phase boundaries from each measurement are consistent, displaying three major phases: a high-temperature paramagnetic paraelectric phase, the AFM 1 below  $T_{N1} = 36$  K, and AFM 2 below  $T_{N2} = 24$  K. In particular, we find evidence of finite electric polarization and ferroelectricity for  $H//c$  above 6 T with a concomitant, sharp SF transition. Thus, we represent the ferroelectric phase realized for  $H//c$  above 6 T as SF 1 and FE. Moreover, for  $H//a$ , we find two SF-like transitions inside the AFM 2 phase, and the resulting phases are termed SF 1' and SF 2. In particular, in the SF 1' region, we observe the ferroelectric polarization along the  $a$ -axis, as summarized in Fig. 4b.

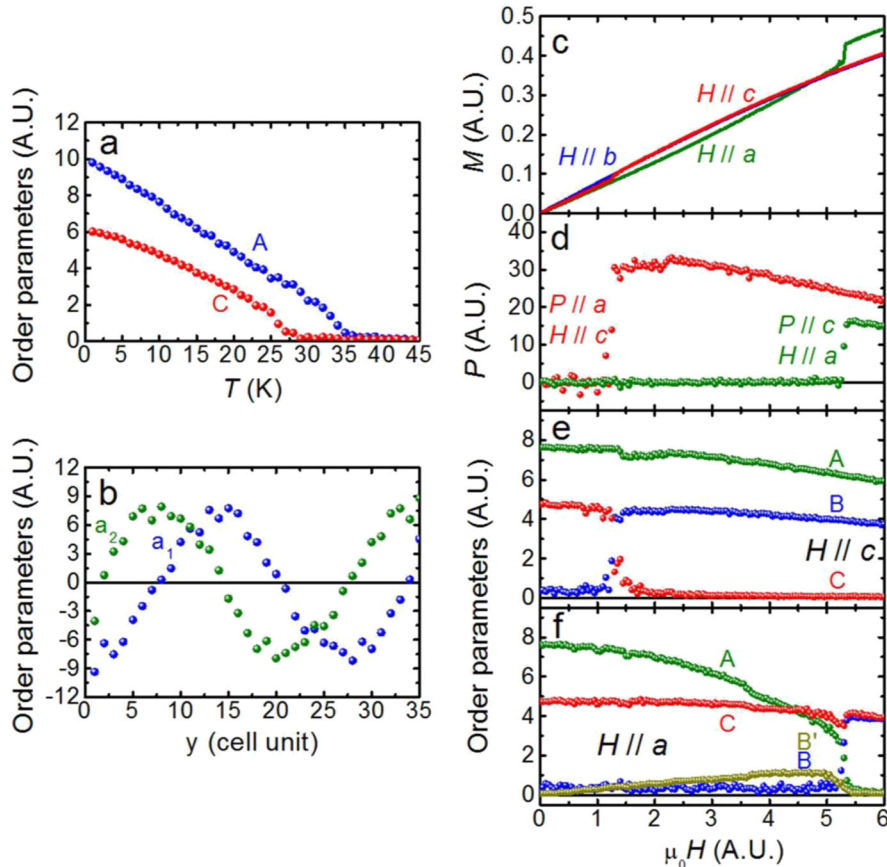
In order to understand the possible magnetic structures in each phase and the  $H$ -induced electric polarization, we conducted classical MC simulations using the exchange constants, which

were determined by the DFT calculation as described in the Methods section and are summarized in Table 1. The studied compound contains magnetic ions with lowest possible spin ( $S = 1/2$ ) and, therefore, a variant of quantum MC simulations possibly would have been better suited to study its magnetic properties. However, we use here classical MC calculations to obtain a qualitative picture and use the results such as modulation wave vectors as inputs for the symmetry analysis of ME interactions described below. The results of MC simulations supported by the symmetry analysis are in good agreement with the experimental findings. The model Heisenberg Hamiltonian has the form,

$$\mathcal{H} = \sum_{\langle ij \rangle} J_{ij} \vec{S}_i \cdot \vec{S}_j + \sum_i (K_x S_{ix}^2 + K_y S_{iy}^2 + K_z S_{iz}^2) - \sum_i \vec{H} \cdot \vec{S}_i, \quad (1)$$

where the spins  $\vec{S}_i$  are classical vectors of unit length,  $\vec{H}$  is the magnetic field,  $K_a$  ( $a = x, y, z$ ) are anisotropy constants, and we assume that the axes  $x$ ,  $y$ , and  $z$  are along the  $a$ -,  $b$ -, and  $c$ -directions, respectively. According to the succession of anomalies in the  $\chi(T)$  data, one can conclude that  $K_x < K_z < K_y$ . We find that the simulation results based on the values  $K_x = -1$  meV,  $K_y = 0.05$  meV, and  $K_z = 0$  could provide qualitative correspondence with the experiments. Preliminary simulations of  $20 \times 20 \times 20$  unit cells (96,000 magnetic ions) first identified that the magnetic structure is modulated along the  $b$ -direction with a wave vector close to  $\vec{k} = (0, \frac{1}{3}, 0)$ . Therefore, subsequent studies were performed using the  $4 \times 75 \times 4$  simulation box.

In order to understand the magnetic structure and its coupling to the electric polarization, we performed a symmetry analysis. In the  $\vec{k} = (0, \frac{1}{3}, 0)$  point of the Brillouin-zone, the  $Pnma$  space group has four two-dimensional irreducible representations (IRs)  $\Delta_i$  ( $i =$



**Fig. 5** Results of the MC simulation on  $\text{PbCu}_3\text{TeO}_7$ . **a** Temperature dependence of order parameter amplitudes A and C at a zero-applied magnetic field, **b** spatial variation of the order parameters ( $a_1$ ,  $a_2$ ) along the  $b$ -direction, and **c** the magnetization, **d** polarization, and **e**, **f** order parameters as functions of the magnetic field along various directions

1,2,3,4). The magnetic structure belongs to the  $\Delta_2 \otimes V'$  exchange multiplet (here  $V'$  is the pseudo-vector representation)<sup>42</sup>. This multiplet splits into the direct sum of IRs  $\Delta_4$ ,  $\Delta_1$ , and  $\Delta_3$ , according to which the  $x$ ,  $y$ , and  $z$  components of spins transform, respectively, and we denote the respective order parameters by  $(a_1, a_2)$ ,  $(b_1, b_2)$ , and  $(c_1, c_2)$ .

The appearance of the modulated magnetic structure is in accordance with macroscopic symmetry since it allows the Lifshitz invariants

$$a_1 \frac{a_2}{\partial y} - a_2 \frac{a_1}{\partial y}, \quad b_1 \frac{b_2}{\partial y} - b_2 \frac{b_1}{\partial y}, \quad c_1 \frac{c_2}{\partial y} - c_2 \frac{c_1}{\partial y}, \quad (2)$$

which result in the modulation of magnetic order along the  $b$ -axis.

According to the MC simulations at a zero magnetic field, upon lowering the temperature, the first phase transition occurs at  $T_{N1}^{MC} = 35$  K and shows a spatially modulated order parameter  $(a_1, a_2)$ . Further cooling results in the additional appearance of a spatially modulated  $(c_1, c_2)$  at  $T_{N2}^{MC} = 28$  K. Thus, the AFM 1 phase is sinusoidally modulated, whereas in the AFM 2 phase, spins lie in the  $ac$ -plane, forming a proper screw-type spin order. In the AFM 2 phase, the spin modulation period is approximately 25 unit cells along  $b$ . In spin-ordered phases AFM 1 and AFM 2, the spatially varying order parameters can be approximated with good accuracy by harmonic functions, e.g.,  $a_1 = A \cos(ky + y_0)$  and  $a_2 = A \sin(ky + y_0)$ . Therefore, in the following, we define amplitudes  $A$ ,  $B$ , and  $C$  of the order parameters. The temperature dependence of amplitudes  $A$  and  $C$  is shown in Fig. 5a, whereas an example of a spatially modulated order parameter is presented in Fig. 5b.

The dependence of the magnetization on external  $H$  applied along various directions is shown in Fig. 5c. Upon application of  $H_c$  above  $\approx 1.2$  A.U., the plane of spin rotations changes into the  $ab$ -plane and becomes perpendicular to the magnetic field as shown in Fig. 5e. This cycloidal spin structure is described by spatially modulated  $(a_1, a_2)$  and  $(b_1, b_2)$  and possesses electric polarization along  $a$  due to the ME interaction

$$(a_1 b_1 + a_2 b_2) P_a, \quad (3)$$

in accordance with the experimental results for the SF 1 phase.

However, the application of  $H_a$  results in a more complex behavior. The symmetry allows the interaction

$$(a_1 b_1 c_2 + a_1 b_2 c_1 + a_2 b_1 c_1 - a_2 b_2 c_2) M_a, \quad (4)$$

where  $M_a$  is the macroscopic magnetization along the  $a$ -axis. According to interaction (4), in the presence of the order

parameters  $(a_1, a_2)$  and  $(c_1, c_2)$ , the application of  $H_a$  induces a spatially varying order parameter that is modulated with a wave vector twice that of  $(a_1, a_2)$  and  $(c_1, c_2)$  and which we denote by  $(b'_1, b'_2)$  to distinguish it from  $(b_1, b_2)$  modulated with the same  $k$ . The order parameters  $(b_1, b_2)$  and  $(b'_1, b'_2)$  have the same symmetry; however, according to the results of the MC calculations, the latter describes the magnetic moment components along the  $c$ -axis and is given by

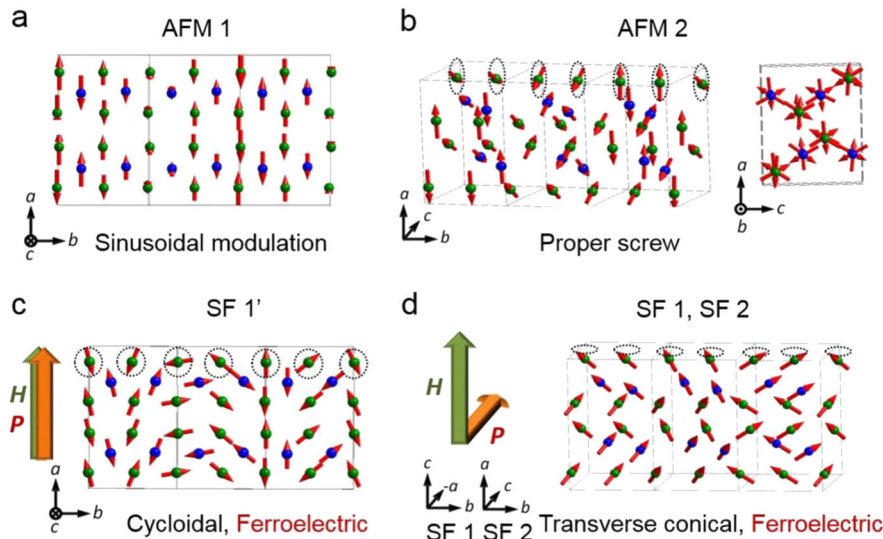
$$b'_1 \sim (a_1 c_2 + a_2 c_1) M_a, \quad (5)$$

$$b'_2 \sim (a_1 c_1 - a_2 c_2) M_a, \quad (6)$$

thus being proportional to  $H_a$ . Here, we have  $b'_1 = B' \cos(2ky + y_0)$  and  $b'_2 = B' \sin(2ky + y_0)$ . The field dependences of  $A$ ,  $B$ ,  $B'$ , and  $C$  are shown in Fig. 5f. Due to the fact that  $(b'_1, b'_2)$  is modulated with a doubled wave vector, its appearance with the application of  $H_a$  does not result in the emergence of electric polarization because the ME interaction represented by Eq. 3 averages to zero after the integration over the volume of the crystal. Therefore, model Hamiltonian (1) alone cannot explain the observation of  $P_a$  in the SF 1 phase realized under intermediated  $H_a$ .

However, our MC simulations show that further increases in  $H_a$  above  $\approx 5.3$  A.U. eventually results in an SF transition, at which the plane of rotation changes to the  $bc$ -plane, as shown in Fig. 5f, being consistent with the experiments identifying the SF 2 phase. At intermediate  $H_a < 5.3$  A.U., it is possible to observe another field-induced phase transition, which can result either in a phase with all order parameters  $(a_1, a_2)$ ,  $(b'_1, b'_2)$ , and  $(c_1, c_2)$  being commensurate and non-zero or in an incommensurate phase with order parameters  $(a_1, a_2)$  and  $(b'_1, b'_2)$  modulated with the wave vector  $k$  and  $(c_1, c_2)$  with  $2k$ . Both possible phases will result in the emergence of  $P_a$  owing to Eq. 3. Such a field-induced phase transition can result from more complex magnetic anisotropies present in  $\text{PbCu}_3\text{TeO}_7$ , which are not captured in our simplified Hamiltonian. Thus, it represents a transition to a phase intermediate between the zero-field,  $ac$  proper screw, and high-field,  $bc$  cycloidal structures. Neutron diffraction studies are required in order to clarify the spin structure of this intermediate field-induced phase.

All of the spin structures obtained by the MC simulations are summarized in Fig. 6. In the ferroelectric phase, the spin structure is cycloidal and the spontaneous  $P$  emerges along the  $a$ -axis. The microscopic origin of  $P_a$  can be revealed by rewriting Eq. 3 in



**Fig. 6** Schematics of spin arrangements in the **a** AFM 1, **b** AFM 2, **c** SF 1', and **d** SF 1 and SF 2 phases in  $\text{PbCu}_3\text{TeO}_7$ . All the spin components were drawn based on the results of the MC simulations



terms of spins. The corresponding analysis shows that  $P_a$  arises due to contributions from both single-spin, described, e.g., by  $p$ - $d$  hybridization model, and two-spin interactions, possessing vector spin products. The latter can be interpreted as IDM<sup>22</sup> or spin current<sup>24</sup> models. In the spin current model, the local electric polarization is expressed by

$$\mathbf{P}_{ij} \propto \mathbf{e}_{ij} \times (\mathbf{S}_i \times \mathbf{S}_j), \quad (7)$$

where  $\mathbf{e}_{ij}$  is the propagation vector between  $\mathbf{S}_i$  and  $\mathbf{S}_j$ . In  $\text{PbCu}_3\text{TeO}_7$ ,  $\mathbf{e}_{ij}$  is along the  $b$ -direction and the spin current  $\mathbf{j}_s (= \mathbf{S}_i \times \mathbf{S}_j)$  is along the  $c$ -direction. Thus, the spin current model predicts the direction of  $\mathbf{P}_{ij}$  ( $= \mathbf{e}_{ij} \times \mathbf{j}_s$ ) to be along the  $a$ -axis, consistent with the experimental results. In addition, the polarizations  $\mathbf{P}_{ij}$  between each of the two spins have the same direction in the cycloidal order, which thus results in the macroscopic electric polarization  $P_a$ .

In the SF 2 phase realized under  $H//a$  higher than 38 T, the spin rotation plane flips to the  $bc$ -plane. However, as the magnetic field is high, spins do not lie only in the  $bc$ -plane, but also are canted to the  $a$ -direction, resulting in the field-induced transverse conical (TC) spin order. In principle, the TC spin order should give rise to electric polarization  $P$  along the  $c$ -direction according to the spin current model. Macroscopic symmetry also allows a form of the ME interaction

$$(b_1c_2 - b_2c_1)P_c \quad (8)$$

The MC simulations show that at  $H_a > 5.3$  A.U., the modulated order parameters  $(b_1, b_2)$  and  $(c_1, c_2)$  develop in a way that homogenous  $P_c$  arises owing to Eq. 8. Thus, this TC phase is ferroelectric with the polarization along the  $c$ -direction. In the experiments, however, we have not confirmed  $P//c$  yet as the pulsed field experiments have been so far performed only at the  $P//a$  configuration.

## DISCUSSION

The geometric spin frustration inherent to the kagome lattice generically suppresses the static long-range spin order. Therefore, ME/multiferroic properties, which are mostly coupled to a specific spin ordering, are rare in the kagome structure. However, the "distorted" kagome structures including the kagome staircase can relieve the degree of spin frustration either by anisotropic distortion in the kagome intralayer or by developing an interlayer interaction. As a result, several multiferroic/magnetolectric compounds with the "distorted" kagome structures is characterized by only moderate spin frustration; for example, the ratio between the Curie–Weiss temperature and the Neel temperature  $\theta_{CW}/T_N$  is  $\sim 2$  in  $\text{KCu}_3\text{As}_2\text{O}_7(\text{OD})_3$ ,  $\sim 3.3$  in  $\text{Ni}_3\text{V}_2\text{O}_8$ , and  $\sim 4$  in  $\text{PbCu}_3\text{TeO}_7$ . More importantly, such "distorted" kagome materials possess significant competing next-nearest interaction, which can often produce noncollinear spin orderings that are directly linked to their ferroelectric and ME properties. Therefore, significant exchange interactions beyond the first neighbors and the lifted geometric spin frustration should be regarded as common key features relevant for both  $\text{Ni}_3\text{V}_2\text{O}_8$  and the presently studied  $\text{PbCu}_3\text{TeO}_7$ .

In recently reported multiferroic  $\text{KCu}_3\text{As}_2\text{O}_7(\text{OD})_3$ <sup>37,38</sup> with monoclinic two-dimensional kagome planes, the anisotropic intralayer distortion plays a dominant role in stabilizing a noncollinear spin ordering; it has nearly perfect two-dimensional kagome planes with the ratio of intralayer to interlayer interaction  $J_{\text{inter}}/J_{\text{intra}} \sim 0.01$ .<sup>37</sup> However, its intralayer distortion is significant enough to give rise to a high ratio of the intralayer lattice constants  $a/b$  of  $\sim 1.72$ , thus relieving the geometric frustration in the kagome plane considerably and resulting in a long-range magnetic ordering below 7 K.

However, kagome staircase compound  $\text{PbCu}_3\text{TeO}_7$  studied here exhibits a much higher  $J_{\text{inter}}/J_{\text{intra}} \sim 1$  (Table 1), thereby more

strongly mitigating spin frustration through the interlayer coupling. Owing to the inherent characteristic of the kagome staircase structure, the ratio of the intralayer lattice constants  $c/b$  of  $\sim 1.4$  in  $\text{PbCu}_3\text{TeO}_7$  is still high enough to cause further reduction in the degree of spin frustration. The situation for kagome staircase compound  $\text{Ni}_3\text{V}_2\text{O}_8$  is similar;  $J_{\text{inter}}/J_{\text{intra}} \sim 0.4$ <sup>9</sup> and the ratio of the intralayer lattice constants is  $\sim 1.39$ <sup>13</sup>. Therefore, both  $\text{PbCu}_3\text{TeO}_7$  and  $\text{Ni}_3\text{V}_2\text{O}_8$  have a high number of considerable magnetic exchange interactions, which act together to reduce the geometric spin frustration and result in long-range incommensurately modulated magnetic ordering. External magnetic field perturbs the three-dimensional magnetic interactions in these staircase kagome compounds, which results in complex phase diagrams together with rich anisotropic behavior, as found in  $\text{PbCu}_3\text{TeO}_7$  as well as in  $\text{Ni}_3\text{V}_2\text{O}_8$ .

The phase diagram of  $\text{PbCu}_3\text{TeO}_7$  can be compared with that of  $\text{Ni}_3\text{V}_2\text{O}_8$ , where  $S=1$  and a cycloidal spin ordering is stabilized between 4 and 6.3 K in the low-temperature insulating phase. As another staircase kagome compound with  $S=1/2$ ,  $\text{PbCu}_3\text{TeO}_7$  similarly exhibits a kind of noncollinear spin ordering, i.e., a proper screw-type spin ordering, below  $T_{N2} = 24$  K at a zero magnetic field. Both staircase compounds also form a collinear sinusoidal spin ordering at high temperatures above their noncollinear spin orderings. In this sense, they share close similarities in the spin ordering patterns. Furthermore, both compounds share another similarity of displaying complex electric/magnetic phase diagrams that are considerably different for each  $H$  direction.

However,  $\text{Ni}_3\text{V}_2\text{O}_8$  has additional magnetic anisotropy, so that its spin rotation planes contain the spin propagation direction parallel to the Ni spins, forming a cycloid spin structure. Moreover, it exhibits two kinds of canted AFM order below 4 K, whereas  $\text{PbCu}_3\text{TeO}_7$  maintains a proper screw-type spin ordering below  $T_{N2}$ , whose spin rotation plane is perpendicular to the spin propagation direction parallel to Cu spines. Therefore, in  $\text{PbCu}_3\text{TeO}_7$ , the magnetic field is used to control effective magnetic anisotropy to further induce SF transitions and resultant spin cycloid phases with ferroelectric polarization. This fundamental difference in their magnetic anisotropy may stem from the fact that  $\text{Ni}_3\text{V}_2\text{O}_8$  possesses a larger spin value ( $S=1$ ) than  $\text{PbCu}_3\text{TeO}_7$  ( $S=1/2$ ), thereby exhibiting additional sources of magnetic anisotropy due to zero-field splitting and stronger spin–orbit interactions. This may also explain why the polarization is larger in  $\text{Ni}_3\text{V}_2\text{O}_8$  ( $\sim 60 \mu\text{C}/\text{m}^2$ )<sup>14</sup> than  $\text{PbCu}_3\text{TeO}_7$  ( $\sim 15 \mu\text{C}/\text{m}^2$ ) and why the resultant field vs. temperature phase diagram of  $\text{Ni}_3\text{V}_2\text{O}_8$  looks more complex than that of  $\text{PbCu}_3\text{TeO}_7$ .

Finally, we re-emphasize that the kagome staircase structure with both intralayer distortion and interlayer competing interaction can be a useful platform for searching for new field-induced ferroelectric polarization. In particular, the delicate balance in the magnetic anisotropy in three-dimensionally interacting spin networks can produce rich phase evolutions with various spin structures per different magnetic field directions. Therefore, our observation of field direction-dependent multiferroicity and nontrivial spin patterns in  $\text{PbCu}_3\text{TeO}_7$ , combined with former studies on  $\text{Ni}_3\text{V}_2\text{O}_8$ , points to an opportunity that ample field-induced phases and ME/multiferroic effects can also be found in other staircase kagome structures.

In conclusion, we have investigated the ME properties in new staircase kagome magnet  $\text{PbCu}_3\text{TeO}_7$  with  $S=1/2$   $\text{Cu}^{2+}$  spins. The investigation of electric and magnetic properties has revealed that  $\text{PbCu}_3\text{TeO}_7$  becomes ferroelectric, exhibiting  $P_a$  at  $\mu_0 H_c > 8.3$  T and  $15 \text{ T} < \mu_0 H_a < 38$  T and its field-induced phase transitions are concomitant with the SF transitions. By means of MC calculations, we establish a model of spin structures for each phase that mostly explains the origin of magnetic-field-induced  $P$ . Our investigation reveals that staircase kagome magnet  $\text{PbCu}_3\text{TeO}_7$  based on  $S=1/2$  ( $\text{Cu}^{2+}$ ) is a fertile source of competing interactions that create ferroelectric polarization owing to the realization of various

inhomogeneous spin textures induced by magnetic fields. Further studies of neutron scattering and X-ray diffraction under a high-magnetic field will be helpful to fully identify the spin structures and to understand the origin of ME coupling in each high-field phase.

## METHODS

Single crystals of  $\text{PbCu}_3\text{TeO}_7$  were grown using the flux method. First, a  $\text{PbCu}_3\text{TeO}_7$  polycrystalline sample was prepared by the solid-state reaction method using starting materials  $\text{PbO}$ ,  $\text{CuO}$ , and  $\text{Te}$ . They were ground with a molar ratio of 1: 3: 1 and synthesized at  $750^\circ\text{C}$  for 5 days with three intermediate grindings. In order to grow single crystals, the polycrystalline of  $\text{PbCu}_3\text{TeO}_7$  and  $\text{NaCl/KCl}$  flux was mixed with a molar ratio of  $\text{PbCu}_3\text{TeO}_7$ :  $\text{NaCl}$ :  $\text{KCl}$  equal to 1: 10: 10. The mixture was heated at  $800^\circ\text{C}$  for 24 h and then cooled to  $650^\circ\text{C}$  at a rate of  $1^\circ\text{C/h}$ . The single crystals were extracted by washing with hot water.

For the electric measurements, we shaped the single crystal into thin plates, whose surface was normal to the crystal  $a$ -axis. The shaped crystal size was quite small with an area of  $0.13\text{ mm}^2$  and a thickness of  $140\ \mu\text{m}$ . The electrodes on both sides of the plate were formed with silver epoxy. We measured the pyroelectric and ME current ( $\alpha dP/dt$ ) using KE617 electrometer and the dielectric constant using AH2550A capacitance bridge at a frequency of 1 kHz. The magnetic properties were collected using a vibrating sample magnetometer (VSM). These measurements were done in the 9 T PPMS<sup>TM</sup> (Quantum Design) and the 14 T Cryogenic<sup>LTD</sup> magnet system in the temperature ( $T$ ) range from 2 K to 50 K.

The high-magnetic field ME current and magnetization measurements, using SR 570 current amplifier and the induction magnetometry technique, respectively, were done in the pulsed magnetic field up to 60 T at the NHMFL pulsed-field facility at LANL. The magnetization values from the pulsed field were calibrated using the VSM data measured in the 9 T PPMS<sup>TM</sup>.

The DFT calculations of the exchange constants in  $\text{PbCu}_3\text{TeO}_7$  were performed using the Vienna Ab initio Simulation Package.<sup>43</sup> We used the GGA+U approach with the on-site repulsion for Cu atoms by the Dudarev method.<sup>44</sup> The value  $U_{\text{eff}} = U - J = 10\text{ eV}$  was chosen similar to other DFT studies of Cu-containing magnetoelectrics.<sup>45,46</sup> The plane-wave cutoff energy of 500 eV was used, whereas the Brillouin-zone was integrated with the  $4 \times 6 \times 4$  mesh determined by the Monkhorst–Pack scheme.<sup>47</sup> In the previous work,<sup>39</sup> the most important exchange paths were studied identifying eight ( $J_1$  to  $J_8$ ) intra and four ( $J_{i1}$  to  $J_{i4}$ ) interkagome plane couplings. In the present work, we calculate the respective exchange constants, which are summarized in Table 1.

## DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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## AUTHOR CONTRIBUTIONS

B.K. prepared the single-crystal samples. K.Y. measured the magnetization and susceptibility in PPMS. K.Y. and W.N. performed the dielectric constant, pyrocurrent, and ME current measurements in a 14 T magnet. K.Y., J.K., F.F.B., V.S.Z., and N.H. measured the magnetization and ME current in the pulsed magnets. A.G. conducted DFT studies and N.T.O. did the MC calculation. K.Y., N.T.O., A.S., and K.H.K. analyzed the

data and wrote the manuscript. K.H.K. devised the project and advised the research. All the authors discussed the results and commented on the manuscript.

## ADDITIONAL INFORMATION

**Competing interests:** The authors declare no competing interests.

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